

Light competition

$$H_{(i)} \quad \text{Height: } H_{(i)} = \min \left[H_{\max(i)} ; \max \left(0.01 ; H_{\max(i)} \cdot \frac{B^C_{(i,shoot)}}{B^C_{\max(i,shoot)}} \right) \right] \quad E18$$

with $B^C_{(i,shoot)} = B^C_{(i,leaf)} + B^C_{(i,stem)}$ and $B^C_{\max(i,shoot)}$ the maximal value of $B^C_{(i,shoot)}$

$$LAI_{(i)} \quad \text{Leaf area index: } LAI_{(i)} = \frac{B^C_{(i,leaf)}}{\chi \cdot LMA_{(i)}} \quad \text{with carbon content } \chi = 0.45 \quad E19$$

$$LAI_{1(i)} \quad \text{Leaf area index in layer 1, linearly related to height (for details see in Appendix II, annexe 1)} \quad E20$$

$$A^1_{h(i)} \quad \text{Light interception: } A^1_{h(i)} = \frac{k_{(i)}}{\sum_{i'} k_{(i')}} \cdot I^1_h \cdot \left[1 - \exp \left(- \sum_{i'} k_{(i')} \cdot LAI_{1(i')} \right) \right] \quad E21$$

$$I^0_h \quad \text{PAR above the canopy at solar time h: } I^0_h = \max \left[I_{\max} \cdot \cos \left(\frac{h-12}{\tau} \cdot \pi \right) ; 0 \right] \quad E22$$

$$I_{\max} \quad \text{Daily maximal instantaneous radiation: } I_{\max} = \frac{\Gamma_U \cdot R_g}{\Gamma_I \cdot \tau} \quad E23$$

with data inputs (R_g : daily radiation and τ : day length) and constants (Γ_U : unit change and Γ_I : integration)

$$I^{1+1}_h \quad \text{Instantaneous PAR above the layer l: } I^{1+1}_h = I^1_h \cdot \exp \left(- \sum_{i'} k_{(i')} \cdot LAI_{1(i')} \right) \quad E24$$

Nitrogen competition

$$U^N_{theo(i)} \quad \text{Potential nitrogen assimilation: } U^N_{theo(i)} = U^C_{theo(i)} \cdot \sum_j \left(f^C_{(i,j)} / \xi_{(i,j)} \right) \quad E25$$

$$V^N_{theo(i)} \quad \text{Plant nitrogen demand: } V^N_{theo(i)} = \max \left(U^N_{theo(i)} - \sum_j \mathfrak{R}^N_{a(i,j)} ; 0 \right) \quad E26$$

$$U^N_{soil(i)} \quad \text{Actual plant uptake: } U^N_{soil(i)} = \min \left(V^N_{theo(i)} ; \frac{SRL_{(i)} \cdot B^C_{(i,root)}}{\sum_{i'} SRL_{(i')} \cdot B^C_{(i',root)}} \cdot \frac{\Delta N_m}{\Delta t} \right) \quad E27$$

N_m Soil mineral nitrogen [$\Delta N_m = N_m$ in limiting nitrogen]

$$U^N_{atm(i)} \quad \text{N-fixing: } U^N_{atm(i)} = (1 - \gamma_{(i)}) \cdot (V^N_{theo(i)} - U^N_{soil(i)}) \quad E28$$

$$U^C_{\max(i)} \quad \text{Actual carbon uptake: } U^C_{\max(i)} = \left(\sum_{j'} \mathfrak{R}^N_{a(i,j')} + U^N_{atm(i)} + U^N_{soil(i)} \right) \cdot \sum_{j'} \left(\xi_{(i,j')} \cdot f^N_{(i,j')} \right) \quad E29$$

5.4 - Seed cycle (cf. Table 4.3).

$$G^C_{s(i)} \quad \text{Seed germination: } G^C_{s(i)} = \begin{cases} \text{if } t = t_{0(i)} \text{ then } G^C_{d(i)} \\ \text{if } t = t_{g(i)} [365] \text{ then } \left[G^C_{r(i)} + (1 - \delta_{(i)}) \cdot H^C_{s(i,seed)} \right] \cdot (1 - \Omega) \end{cases} \quad E30$$

with $\delta_{(i)}$ fraction of seed dispersion; $t_{g(i)}$ time of seed germination and $t_{0(i)}$ time of first germination

$$\Omega \quad \text{Soil cover: } \Omega = 1 - \exp \left(- \sum_{i'} k_{(i')} \cdot LAI_{(i')} \right) \quad E31$$

$$H^C_{s(i,j)} \quad \text{Seed dispersion: } H^C_{s(i,j)} = \left\{ \text{if } t = t_{d(i)} [365] \text{ and } j = \text{seed, then } B^C_{(i,seed)}, \text{ else } 0 \right\} \quad E32$$

with $t_{d(i)}$ time of seed dispersion

5.5 - Nitrogen cycling through soil (cf. Table 4.2 and Figure 4-c).

$$\Delta N_m / \Delta t = \delta + a_{qd} L^N + a_{sd} SOM^N - N_{leached} - U^N_{soil} \quad E33$$

$$\Delta L^N / \Delta t = F^N - a_{qd} L^N - \beta L^N \quad E34$$

$$\Delta SOM^N / \Delta t = \beta L^N - a_{sd} SOM^N \quad E35$$

$$N_{leached} \quad \text{Nitrogen leached: } N_{leached} = \min(\lambda \rho W, \Delta N_m / \Delta t - U^N_{soil}) \quad E36$$

$$U^N_{soil} \quad \text{Plant uptake: } U^N_{soil} = \sum_i U^N_{soil(i)} \quad E37$$

$$F^N \quad \text{Litter fall: } F^N = \sum_i \sum_j F^N_{(i,j)} \quad E38$$

$\beta, \delta, \lambda, \rho, a_{qd}$ and a_{sd} are defined in Table 4.2.