

Fig. 6. Viscous relaxation of Orienteale basin topography for a 100-km-thick layer of viscosity $\eta = 10^{25}$ P over an inviscid half space. Profile times and their scaling with η are as in Figure 5.

1974; Koyama and Nakamura, 1979]. The time constant τ_2 behaves similarly to the time constant (equation (6)) for the case of the viscous layer overlying an inviscid half space of the same density: $\tau_2 \sim k^4$ for small k and is equal to the time constant $\tau_0 \sim k$ for the half-space case at large k . The time constant τ_1 , however, is considerably larger than τ_0 at all wave numbers, particularly at small k . As $k \rightarrow 0$, τ_1 approaches a constant (equation (A33)), a function of ρ , $\Delta\rho$ and H but not of k . At large k , τ_1 is proportional to k and exceeds the half-space time constant by the factor $\rho/\Delta\rho$.

Thus partial to complete isostatic compensation of initial basin topography results in a considerable deceleration of viscous relaxation of relief, compared to models without isostatic effects, for a fraction of the initial relief that depends on the degree of compensation. As shown in equation (A35), the fraction F_1 of F that decays with the time constant τ_1 approaches unity in the long-wavelength limit for complete initial compensation ($c = 1$). Further, for any value of c , the topographic relief decaying with time constant τ_1 is always completely compensated for small k ; i.e., the long-wavelength basin topography is isostatic for $t \gg \tau_2$ no matter what the initial degree of compensation.

These conclusions are illustrated in Figures 8 and 9. The case with complete initial compensation ($c = 1$) is shown in Figure 8. Relaxation of relief is much slower than in Figures 2, 5, or 6, with substantial long-wavelength relief (4 km) remaining after 3 b.y. (10^{17} s) for a layer viscosity of 10^{25} P. Note that in comparison to Figures 2 or 5, the topography in the relaxed profiles is 'smoother.' This is because of the comparatively weak dependence of τ_1 on k (see Figure 7) over the wave numbers of interest; i.e., the rate of relaxation at long wavelengths is greater, compared to the short wavelengths, than for the simple half-space model or for the model with no density contrast at the base of the viscous layer.

The case with initial topography only half compensated by Airy isostasy ($c = 0.5$) is shown in Figure 9. There is a rapid partial relaxation of initial relief (governed by time constant τ_2), followed by a much slower relaxation of the remainder. The total relief at 3 b.y. (for $\eta = 10^{25}$ P) is about 2 km, or half that in Figure 8 at the same time. The case with initially

uncompensated topography, but with a density contrast at the base of the layer, behaves similarly to that in Figure 5 except for a small fraction ($\Delta\rho/\rho_m$) of the long-wavelength topographic relief that relaxes at the longer time constant τ_1 .

The assumptions necessary to derive (8) and (9) and the models shown in Figures 8 and 9 include, from equations (A15) and (A22) and by analogy to relations (7),

$$\begin{aligned} k|F| &\ll 1 \\ k|G| &\ll 1 \\ \left| kF + \frac{\Delta\rho}{\rho} kG \right| &\ll (kH)^3/3 \end{aligned} \tag{10}$$

where $G(k)$ is the Hankel transform of the profile of topographic relief at the base of the layer (see the appendix). Strictly, F and G are the coefficients of $J_0(kr)$ in the summation representation of (8) and in the analogous expression for relief at the bottom of the viscous layer. The first two inequalities hold for the Orienteale profile for all k and all t . The third inequality in (10) holds for a greater range of cases than does the analogous inequality in (7) because G

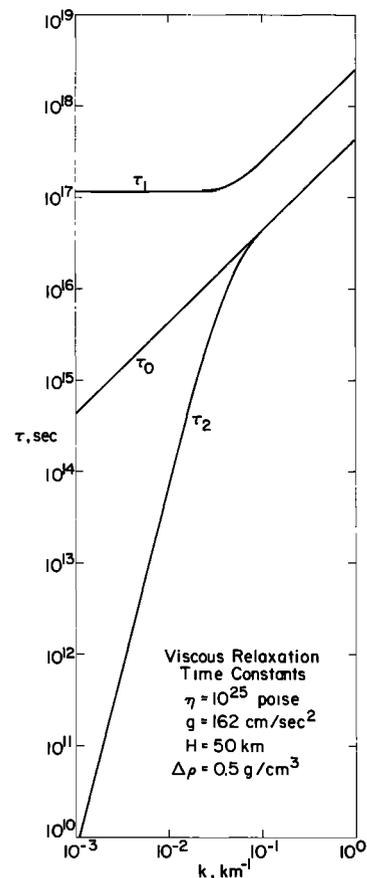


Fig. 7. Time constants τ_1 and τ_2 versus horizontal wave number k for the problem of relaxation of topography on a viscous layer overlying an inviscid half space of greater density, both in a uniform gravitational field. The layer has viscosity $\eta = 10^{25}$ P, density $\rho = 2.9$ g/cm³, and thickness $H = 50$ km; the half space has density $\rho + \Delta\rho = 3.4$ g/cm³; the gravitational acceleration is 162 cm/s². Also shown is the time constant $\tau_0(k)$ for the case of a half space of uniform viscosity η and density ρ . All time constants are proportional to η and inversely proportional to g ; the long-wavelength limit of τ_1 is inversely proportional to H .