

Table 5
SatStress run IDs for figures in this paper.

Fig.	Run ID
3a	20080121182229_4795536555ce9
3b	20080121183751_479556ff3edfa
3c	20080121183841_4795573178a18
3d	20080121183921_479557592a9dc
4a	20080122145730_479674da20bc2
4b	20080122145857_4796753191483
4c	20080122150014_4796757e38a13
4d	20080122150135_479675cfe6ef0
5b	20080123194857_47980aa9b37a4
5d	20080123191023_4798019f7b218

to keep track of every parameter involved in a calculation, and we hope it will facilitate future collaboration.

Acknowledgments

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Appendix A. Tidal potential

Let (r, θ, ϕ) be the spherical coordinates (r = radius, θ = colatitude, ϕ = longitude) of a point in the satellite. The general form of the tidal potential at (r, θ, ϕ) caused by an external point mass (the parent planet), is given in Eq. (1) of Kaula (1964) (changing some of the variable names):

$$\begin{aligned}
 V_T(r, \theta, \phi) = & \frac{Gm^*}{a^*} \sum_{l=2}^{\infty} \left(\frac{r}{a^*}\right)^l \sum_{m=0}^l \frac{(l-m)!}{(l+m)!} (2 - \delta_{0m}) \\
 & \times P_{lm}(\cos \theta) \sum_{p,q} F_{lmp}(i^*) G_{lpq}(\epsilon) \\
 & \times \left[\cos(m\phi) \begin{cases} \cos \\ \sin \end{cases} \right]_{l-m=\text{even}}^{l-m=\text{odd}} \{ (l-2p)\omega^* \\
 & + (l-2p+q)M^* + m(\Omega^* - \Theta^*) \} \\
 & + \sin(m\phi) \begin{cases} \sin \\ -\cos \end{cases} \right]_{l-m=\text{even}}^{l-m=\text{odd}} \{ (l-2p)\omega^* \\
 & + (l-2p+q)M^* + m(\Omega^* - \Theta^*) \} \Big], \quad (\text{A.1})
 \end{aligned}$$

where the six Keplerian elements that describe the parent planet’s apparent motion are Ω^* (longitude of the ascending node), M^* (mean anomaly), i^* (inclination), a^* (semi-major axis), ω^* (argument of pericenter), and ϵ (eccentricity). Other variables are: Θ^* is the sidereal time of the reference meridian, m^* is the mass of the planet, G is Newton’s gravitational constant, the $P_{lm}(\cos \theta)$ are associated Legendre functions, and the $F_{lmp}(i^*)$ and $G_{lpq}(\epsilon)$ are polynomials given in Tables 2 and 3 of Kaula (1964). For most satellites of interest $r/a^* \ll 1$. For Europa, for example, $r/a \leq 0.0023$. Thus, as is usual, we keep only $l=2$ terms in (A.1). We set $i^* = 0$ (since we are assuming the satellite’s obliquity vanishes), which causes the only non-zero $F_{2mp}(i^*)$ to be $F_{220} = 3$, and $F_{201} = -1/2$. We

assume the eccentricity is small ($\epsilon \sim 0.0094$ for Europa), and expand $G_{lpq}(\epsilon)$ in powers of ϵ keeping terms only up to first order. We set $M^* = nt$ (which is exact for Keplerian orbits), and assume $\Theta^* = (n+b)t$ (Θ^* represents the angular displacement between the vector to the planet and the x -axis in our satellite-fixed coordinate system). By choosing $M^* = nt$, we are defining $t=0$ as the time of periape. Because the inclination vanishes, there is no distinction between Ω^* and ω^* , and only the sum ($\Omega^* + \omega^*$) appears in the final solution. We set this sum to zero, which, together with our assumption that $\Theta^* = 0$ at $t=0$, implies that not only is the satellite at periape at time $t=0$, but its x -axis is pointing toward the planet at that time. The longitude, ϕ , of a point in the satellite is defined as the angle eastward (i.e. counterclockwise as seen from above the rotation axis) from this x -axis. Using expressions for the $P_{lm}(\cos \theta)$ gives:

$$\begin{aligned}
 V_T(r, \theta, \phi, t) = & Z \left(\frac{r}{R_s}\right)^2 \left[\frac{1}{6}(1 - 3 \cos^2 \theta) + \frac{1}{2} \sin^2 \theta \cos(2\phi + 2bt) \right. \\
 & + \frac{\epsilon}{2}(1 - 3 \cos^2 \theta) \cos(nt) \\
 & + \frac{\epsilon}{4} \sin^2 \theta [7 \cos(2\phi - (n-2b)t) \\
 & \left. - \cos(2\phi + (n+2b)t) \right], \quad (\text{A.2})
 \end{aligned}$$

where

$$Z = \frac{3Gm^*R_s^2}{2a^{*3}}, \quad (\text{A.3})$$

and R_s is the radius of the satellite.

The last two terms on the right-hand side of Eq. (A.2) have angular frequencies of $(n-2b)$ and $(n+2b)$, respectively. Because b (the rate of NSR) is much smaller than n (the mean motion; which, for a satellite in near-synchronous rotation, is about equal to the diurnal rotation rate), we can ignore b in both those frequencies. In that case, V_T reduces to Eq. (1) in the main text, reproduced here:

$$V_T(r, \theta, \phi, t) = Z \left(\frac{r}{R_s}\right)^2 [T_* + T_0 + T_1 + T_2], \quad (\text{A.4})$$

given that

$$T_* = \frac{1}{6}(1 - 3 \cos^2 \theta), \quad (\text{A.5})$$

$$T_0 = \frac{1}{2} \sin^2 \theta \cos(2\phi + 2bt), \quad (\text{A.6})$$

$$T_1 = \frac{\epsilon}{2}(1 - 3 \cos^2 \theta) \cos(nt), \quad (\text{A.7})$$

$$T_2 = \frac{\epsilon}{2} \sin^2 \theta [3 \cos(2\phi) \cos(nt) + 4 \sin(2\phi) \sin(nt)]. \quad (\text{A.8})$$

Appendix B. Surface stresses for elastic satellites

The stress tensor associated with the tidal displacement vector, is given by Eq. (8) in the main text:

$$\tau = \lambda(\nabla \cdot \vec{s}) + \mu[\nabla \vec{s} + (\nabla \vec{s})^T]. \quad (\text{B.1})$$

We use this relation, together with the surface displacement components first defined in Eqs. (9)–(11):

$$s_r(r = R_s, \theta, \phi, t) = \left(\frac{h}{g}\right) V_T \Big|_{r=R_s}, \quad (\text{B.2})$$

$$s_\theta(r = R_s, \theta, \phi, t) = \left(\frac{\ell}{g}\right) \frac{\partial V_T}{\partial \theta} \Big|_{r=R_s}, \quad (\text{B.3})$$

$$s_\phi(r = R_s, \theta, \phi, t) = \left(\frac{\ell}{g \sin \theta}\right) \frac{\partial V_T}{\partial \phi} \Big|_{r=R_s} \quad (\text{B.4})$$