

is used for each term in the composite rheology (equation 1.38). The resulting flow law for ice I is

$$\frac{1}{\eta_{tot}} = \frac{A_{diff}}{d^2} \exp\left(\frac{-Q_v^*}{RT}\right) + A_{disl} \sigma^3 \exp\left(\frac{-Q_{disl}^*}{RT}\right) + \left(\frac{d^{1.4}}{A_{GBS}} \sigma^{-0.8} \exp\left(\frac{Q_{GBS}^*}{RT}\right) + \frac{1}{A_{bs}} \sigma^{-1.4} \exp\left(\frac{Q_{bs}^*}{RT}\right) \right)^{-1} \quad (1.40)$$

where the stress and grain size exponents for each flow law have been evaluated to highlight the weakly non-Newtonian behavior of grain boundary sliding and basal slip.

To non-dimensionalize the viscosity functions, each term in the composite rheology (equation 1.38) is divided by a reference viscosity defined by the viscosity due to diffusion creep at the melting temperature of ice. The strain rate from diffusion creep is described by

$$\dot{\epsilon} = \frac{A_{DF} V_m \sigma}{RT_m d^2} \left(D_v + \frac{\pi \delta}{d} D_b \right) \quad (1.41)$$

where A_{DF} is the diffusion constant, V_m is the molar volume, T_m is the melting temperature of ice, D_v is the rate of volume diffusion, δ is the grain boundary width, and D_b is the rate of grain boundary diffusion. For small strains of order 1%, $A_{DF} = 42$, but for larger strains $A_{DF} > 42$ (*Goodman et al.*, 1981). Here, $A_{DF} = 42$ is used.

The grain sizes of ice in the satellites are likely much larger than the grain boundary width (9.04×10^{-10} m) (*Goldsby and Kohlstedt*, 2001), so volume diffusion dominates over grain boundary diffusion, and the contribution to the strain rate by grain boundary diffusion is negligible. The strain rate for volume diffusion is:

$$\dot{\epsilon} = \frac{42 V_m \sigma}{RT_m d^2} D_{o,v} \exp\left(\frac{-Q_v^*}{RT}\right) \quad (1.42)$$

where $D_{o,v}$ is the volume diffusion rate coefficient and Q_v^* is the activation energy. The parameters for volume diffusion are listed in Table A.2, where the pre-exponential parameters have been grouped as $A = (42 V_m D_{o,v} / RT_m)$. The viscosity due to volume diffusion is, therefore,

$$\eta_o = \frac{d^2}{A} \exp\left(\frac{Q_v^*}{RT_m}\right). \quad (1.43)$$