



Figure 5. Total factor productivity as a function of the market interest rate ( $\alpha = 0.033$ )

Such an exercise is of interest given Valerie Ramey's (1989) study of modeling inventories as a factor of production. Indeed, we can give a Cobb-Douglas representation as follows. Note from (12) that total output can be written as

$$\begin{aligned}
 Y(K, L) &= n^\alpha L \\
 &= \left( \frac{2K}{wL} - 1 \right)^\alpha L \\
 &= \left( \frac{2}{w} - \frac{L}{K} \right)^\alpha K^\alpha L^{1-\alpha}
 \end{aligned} \tag{15}$$

Imposing a Cobb-Douglas functional form for working capital will result in a misspecified production function, where total factor productivity depends on endogenous variables.

Figure 5 plots the TFP term in the production function as a function of the borrowing rate  $r$  when  $\alpha = 0.033$ . The TFP term is not well-defined when  $r = 0$ , since both expressions inside the brackets in (15) shoot off to infinity. However, for reasonable ranges for  $r$ , the TFP term is decreasing in the borrowing rate.

To an outside observer who imposes a Cobb-Douglas production function